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Computational investigation of the effect of thermal perturbation on the mechanical unfolding of titin I27

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Abstract The emergence of single-molecule force measurement experiments has facilitated a better understanding of protein folding pathways and the thermodynamics involved. Computational methods such as steered molecular dynamics (SMD) simulations are helpful in providing atomistic level information on the unfolding pathways. Recent experimental studies have showed that combinations of single-molecule experiments with traditional methods such as chemical and/or thermal denaturation yield additional insights into the folding phenomenon. In this study, we report results from extensive computations (a total of about 60 SMD simulations with a total length of about 0.4 µs) that address the effect of thermal perturbation on the mechanical stability of the I27 domain of the protein titin. A wide range of temperatures (280-340 K) were considered for the pulling, which was done at both constant velocity and constant force using SMD simulations. Good agreement with experimental data, such as for the trends in changes in average force and the maximum force with respect to the temperature, was obtained. This study identifies two competing pathways for the mechanical unfolding of I27, and illustrates the significance of combining various techniques to examine protein folding.

Keywords Protein folding · Steered molecular dynamics · Denaturation · Mechanical stability · Titin I27 · Folding pathways

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Introduction

During the past two decades or so, single-molecule force measurements using atomic force microscopy (AFM) have been extensively used to study protein folding [1-4]. Typically, a single molecule of the biomolecule under study is tethered between the AFM cantilever and its stage, and stretched at a known speed while simultaneously measuring the force. Similar methods have also been used to investigate RNA folding and aptamer-ligand binding [5–7]. Recently, the applicability of single-molecule experiments to investigations elucidating the biological activities of inhibitors and the design of new ligands has been demonstrated using SMD simulations [8]. These singlemolecule manipulation techniques allow the characterization of not only the folded and unfolded states but also the intermediate states along the folding pathway [2]. The order parameter or the reaction coordinate for unfolding in these experiments is usually the distance between the terminal residues. However, the order parameter for protein folding is not necessarily this inter-residue distance. Hence, it is important to validate the applicability of these methods to study the structure-function relationships of a given biomolecule. Traditionally, chemical denaturants such as guanidinium chloride and thermal perturbation along with spectroscopic methods have been used to study protein folding [9]. Recent studies have shown that it is important to combine single-molecule experiments with either chemical denaturants or with thermal perturbations to study folding processes [10-14]. They proposed that such combinations of multiple techniques along with comparisons of results from multiple probes are useful for validating the protocol used [12]. Additionally, they provide an opportunity to explore various aspects of protein folding that may not be accessible by any of these methods when used individually. Theoretical studies have already been performed to include temperature as a variable while investigating the mechanical stability of proteins and RNA [15–17].

Titin is a huge protein consisting of about 30,000 amino acids that has been shown to be crucial to the contraction and stretching of muscle [20]. The mechanical (un)folding of titin I27 has been extensively studied both experimentally, using single-molecule approaches [21–23], and computationally [24–31]. The structure of I27 consists of two sheets: β strands A, B, E, and D form the first sheet, and β -strands A', G, F, and C form the second sheet (Fig. 1). Schulten and coworkers have investigated the molecular level details of the force-induced unfolding of I27 using SMD simulations [24–26]. They have calculated force vs. extension profiles that are consistent with experimental data. They showed that the force peak observed at around 13 Å corresponds to the loss of interactions between the A and B and the A' and G strands [24].

In the present study, we attempt to understand the effect of temperature on the mechanical unfolding of the titin I27 domain using SMD simulations. The protein was selected based on recent experimental studies of this protein [11, 13], and the validity of the end-to-end distance as the order parameter for the unfolding of this protein. Botello et al. showed that the free-energy barrier during the mechanical unfolding of I27 decreases linearly with respect to increasing



Fig. 1 a Secondary structure of titin 127. The two β -sheets are shown as *black and gray colored block arrows*, and the individual strands are named according to previous studies. **b** The tertiary structure of 127 (PDB ID: 1TIT) [18], rendered using the VMD program [19]. The β -strands are colored as in **a**, and the two spheres represent the N-terminal and C-terminal C α atoms

temperature and the concentration of the chemical denaturant, guanidinium chloride [11]. A detailed study by Taniguchi et al. illustrated the effect of temperature on the mechanical stress of the native and intermediate states of I27 [13]. They hypothesized that the energy landscape does not alter with respect to temperature until the folded state reaches the intermediate state, although it changes substantially beyond that. The results obtained here are compared with the available experimental data, and the two show good agreement. Our results support the hypothesis for the energy landscape proposed by Taniguchi et al. [13], and show two competing unfolding pathways whose atomistic details are provided.

Methods

The starting structure for the MD simulations was obtained from an earlier NMR study (PDB ID: 1TIT) [18]. All the MD simulations were performed using the NAMD biomolecular simulation program [32] using the CHARMM27 protein force field along with CMAP corrections [33, 34]. The simulations reported in the present paper were performed in an explicit solvent environment using the modified TIP3P water model. The simulation protocol used was based on previously published methods [26]. In short, the protein was solvated in pre-equilibrated water spheres of radius 35 Å. For the purpose of solvation, water spheres equilibrated at 280, 290, 300, 310, 320, 330, and 340 K were used, and the MD simulations were run at the corresponding temperatures. The systems thus solvated at different temperatures were subjected to 5000 steps of minimization followed by 100 ps of equilibration. During equilibration, the non-hydrogen atoms of the I27 domain were restrained using a mass-weighted harmonic constraint of 5 kcalmol⁻¹Å⁻². Constant temperature in these simulations was achieved using the Langevin method, and an integration time step of 1 fs was used. The nonbonded interactions were calculated with a distance cut-off of 10 Å, and zero was reached at 13 Å.

SMD simulations at constant velocity were carried out by fixing the C α atom of the N-terminal residue (Leu-1) and applying external force to the C α of the C-terminal residue (Leu-89). The forces were applied by restraining the C α atom of the C-terminus to a restraint point along the line joining the N-terminal and C-terminal C α atoms at a constant velocity of 0.1 Åps⁻¹. A spring constant (*k*) of 10 kcalmol⁻¹Å⁻² with an integration time of 1 fs was used in the constant-velocity SMD simulations. For a given value of *k*, the fluctuations in the position of the restrained atom are given by $\delta x \sim (k_b T/k)^{1/2}$. Thus, by selecting a very high value of *k* (stiff spring, 10 kcalmolÅ⁻²), the fluctuations in the position of C α of the C-terminal residue are of the order of 0.24 Å at 280 K and 0.26 Å at 340 K. In contrast, the position fluctuations associated with a soft spring with low k values will be much larger [35]. However, it should be noted that the cantilever stiffness used in typical AFM experiments is about two orders of magnitude smaller than the stiffness due to the spring constant used here. Similar to this study, previous studies have used a similar stiff spring to account for the large fluctuations in the positions otherwise [26]. The SMD simulation for each system was continued until the protein formed the completely extended form that resulted in a rapid increase in the unfolding force. The SMD output, including the force vector and the coordinates of the C-terminal atom (i.e., the SMD atom), was saved every 10 fs. Five independent simulations with different sets of initial velocities were performed at each of the temperatures given above. An extra set of SMD simulations were carried out at four temperatures (280, 300, 320, and 340 K) and a lower velocity, 0.01 Åps^{-1} . Work done was calculated by integrating the forces as given by the following equation for each trajectory and averaging over the five trajectories at each temperature [36]:

$$W(t) = v \int_0^t dt f(t), \tag{1}$$

where v is the pulling velocity, f(t) is the force required as a function of time to unfold the protein, and t is the time.

SMD simulations were also performed by fixing the N-terminus and applying a constant force of 750 pN to the $C\alpha$ atom of the C-terminal residue in the direction of the

Fig. 2 a Force–extension profiles obtained from constant-velocity SMD simulations of I27 obtained at seven different temperatures.
b Probability distributions of the unfolding forces (*gray lines*) obtained at the corresponding temperatures, including the curves fitted to Gaussian functions (*black lines*). Data from one of the five simulations at each temperature are given (see Figs. S1–S7 in the ESM) line joining the two atoms. Similar to the constant-velocity SMD simulations, five independent simulations were carried out with different sets of initial velocities at four different temperatures (280, 300, 320, and 340 K). The error bars shown at each of the temperatures in the figures represent the standard error of the mean from the five independent observations. It should be noted that the estimates for the errors were calculated based on only five data points in each case, so they must be treated as rough estimates of the true errors. Overall, about 60 independent simulations were done that lasted for about 0.4 µs. The results obtained here are based on the simulations employing the CHARMM force field [33, 34]. All-atom CHARMM protein force field parameters have been shown to adequately represent the inter- and intramolecular forces in protein molecules in general [37]. However, it should be noted that these parameters were developed based on individual amino acids and small peptides, and benchmarked over a test set of proteins [38]. It was recently shown that even small errors in the potential energy functions tend to accumulate for large protein structures, and may result in not very accurate descriptions of the global minima [39]. This may be a crucial factor when using the potential energy functions in ab initio predictions of folded states.

Results and discussion

The present study was primarily motivated by recent experimental studies that employed a combination of



mechanical unfolding using AFM along with thermal or chemical denaturation to study protein folding [11–13]. Here, we attempt to examine the importance of such studies to improve our understanding of protein folding by providing molecular level details of the effect of temperature on the mechanical unfolding of the titin I27 domain. In the current section, the differences in the unfolding of this protein at different temperatures, and their relevance to the experimental studies, are presented.

Force vs. extension profiles were obtained at different temperatures (280-340 K) using the constant-velocity SMD simulations. Select profiles from five independent simulations at each temperature are given in Fig. 2a (see Figs. S1-S7 in the "Electronic supplementary material," ESM, for all the data). The force-extension profiles obtained from the SMD simulations performed at the seven different temperatures were found to be qualitatively similar with respect to each other. However, quantitative differences in the magnitudes of the unfolding forces were observed. As noted before by Schulten and coworkers, the magnitudes of the forces obtained here are higher than those observed under experimental conditions due to the difference in the velocity at which the protein is extended [26]. The force vs. extension profiles were also obtained at a lower velocity (0.01 Åps^{-1}) , and the qualitative trends obtained are similar to those obtained by Schulten and coworkers for a velocity of 1 Åps^{-1} , and for a velocity of 0.1 Åps^{-1} (this work). Though the pulling speed used in the experiments is about six orders of magnitude less than the slowest velocity used here, similar results at the three different velocities indicate that the conclusions arrived at based on these results are possibly independent of the velocity in this range. It is not practical to perform the computations at a lower velocity. To examine the effect of temperature on the overall mechanical resistivity of the protein, probability distributions of the unfolding forces were computed (Fig. 2b, and Figs. S1-S7 in the ESM). All the histograms thus obtained follow a near-Gaussian distribution with properties that change with the temperature at which the MD simulations were performed. The probability distributions of the unfolding forces were fitted to Gaussian functions (Fig. 2b) using standard fitting tools.

The most probable unfolding force, the force at which the probability is maximum based on the Gaussian fit to the distribution, decreases linearly with increasing temperature (Fig. 3a). The values decrease from about 640 to about 425 pN for temperatures of 280 to 340 K. The results from the five independent SMD simulations performed at each of the seven temperatures studied here yielded similar results. The error bars shown at each of the temperatures in the figures represent the standard error of the mean based on five independent observations. This is in excellent agreement with a recent study by Botello et al., which showed that the



Fig. 3 a The change in the most probable unfolding force (force at the maximum probability) with temperature. The best possible linear fit is also given. **b** Peak force obtained from force–extension profiles attained at different temperatures, along with the linear fit. **c** Work vs. extension profiles obtained at different temperatures (K) using the constant velocity 0.1 Å ps^{-1}

peak position of the force distribution moves towards lower forces with increasing temperature [11]. Interestingly, while the unfolding forces are strongly dependent on the temperature, the simulations show that the extension at Fig. 4 Changes in the hydrogen bond donor-acceptor distances [1 F73(N)-S80(O), 2 S80(N)-F73(O), 3 A75(N)-A78(O), 4 A78(N)-A75(O), 5 A19(N)-L60(O), 6 L60(N)-A19(O), 7 F21(N)-L58(O), 8 L58(N)-F21 (O), 9 I23(N)-H56(O), 10 H56 (N)-I23(O), and 11 L25(N)-K54(O)] between strands F and G (black lines) and B and E (grav lines), as calculated from two different trajectories that follow the two competing unfolding pathways. In a, FG unfolds before BE, and in b, BE unfolds before FG



Extension, Å

which the maximum force is required during the unfolding process remains largely unchanged. The distance at which a peak is observed in each force-extension profile can be found in the range 10-13 Å at all temperatures (Fig. S8 in the ESM). Such a similarly positioned transition state in all of the simulations further validates the order parameter of end-to-end distance for the unfolding of I27. Substantial deviations would be expected if the order parameter for unfolding is not the same in thermal denaturation [40]. The present results indicate that the magnitude of the maximum force in the force-extension profiles varies with temperature (Fig. 3b). The unfolding force at the peak in the forceextension profile decreases approximately linearly with increasing temperature. Since the protein softens with increasing temperature, the force required to unfold the protein including the peak force decreases. Notable deviations are the maximum forces obtained at 320 and 340 K. The effect of temperature on the mechanical stability of titin I27, as discussed above, was further validated by another set of constant-velocity SMD simulations done at a lower velocity (0.01 Åps^{-1}) and at four temperatures (280, 300, 320, and 340 K). The trends for the changes in the average and the maximum forces of unfolding, and the extension at maximum force, were found to be consistent with the observations noted above.

The work done corresponding to protein unfolding was calculated by integrating the forces and averaging over the five different trajectories at each of the seven temperatures. Since the work done through extension depends on the pulling velocity, it is appropriate to compare the qualitative changes in the profiles with respect to temperature (Fig. 3c). The work profiles obtained at all seven temperatures at a pulling velocity of 0.1 Åps^{-1} are very similar up



Fig. 5 a The time required to cross the barrier in constant-force pulling experiments decreases with increasing temperature. b Unfolding rates from constant-force SMD simulations—calculated from the slopes of extension—time profiles. Here, the unfolding rate corresponds to the rate after crossing the intermediate state on the way to the fully extended state. Each *error bar* represents the standard error of the mean calculated from five different runs at each temperature

to an extension of about 11 Å (approximately the position where the force required to unfold the protein is maximum). Beyond this extension, the work profiles show temperature dependency in the expected order, where the work required to extend the protein is larger at 280 K than at 340 K. Such an interesting change in the trend for the work required to unfold before and after 11 Å supports the hypothesis provided by Taniguchi et al. [13]. They proposed that the energy landscape remains similar with changes in temperature until the unfolding reaches the intermediate state (~9 Å), but it significantly changes after this extension. The work vs. extension profile for the complete range of extensions at the low velocity (0.01 Åps⁻¹) are given in the ESM (Fig. S9). The work profiles show similar trends at both velocities studied, especially in the range up to 50 Å, and are in agreement with the one proposed by Taniguchi et al.

The unfolding pathways that occur for I27 under all conditions (different temperatures and different velocities) were compared with each other and with previously published studies. As observed in earlier studies, the intramolecular interactions between the A' and G strands were found to require a larger force than the others. Initially, the hydrogen bonds between A and B and then A' and G are lost within about 14 Å of extension. The last set of interactions to be disrupted are the hydrogen bonds between the E and D β -strands. However, the order in which the intramolecular interactions between the B and E, F and G, and F and C strands are distorted was found to follow two distinct patterns. The donor-acceptor distances corresponding to the hydrogen bonding between the two pairs of strands obtained from two different trajectories that show different unfolding pathways are given in Fig. 4. In some of the SMD simulations, F-G contacts were found to distort first, followed by B-E contacts accompanied by F-C interactions (Fig. 4a). In the others, B-E strands were found to unfold first, followed by F-G and F-C (Fig. 4b). Results from all of the constant-velocity simulations are provided in Figs. S10-S16 in the ESM. The consistent observation of two different unfolding patterns for the titin I27 domain (as shown in the figure) indicates two competing pathways. It should, however, be noted that the unfolding of the B, E, F, and C β -strands occurs after the unfolding transition state. Notably, such competing pathways have not been reported from previous computational or experimental approaches.

The results discussed above were further validated by performing constant-force (750 pN) SMD simulations at four different temperatures. The unfolding pathways obtained are consistent with the discussion above. From the extension vs. time profiles (Fig. S17), the time required to cross the transition state barrier in each simulation was calculated. This time was found to linearly decrease with increasing temperature (Fig. 5a), consistent with the above discussion. The extension vs. time profiles obtained at

different temperatures were qualitatively similar, indicating that the distance between the terminal residues is a reasonable order parameter for the unfolding of I27, even under thermal denaturation conditions. The rates of unfolding at constant force after the barrier had been crossed were also calculated, and were found to increase linearly with increasing temperature (Fig. 5 b).

Summary

In summary, the current study reports the effect of thermal perturbation on the mechanical stability of the I27 domain of the protein titin using constant-velocity and constantforce SMD simulations. The average and maximum unfolding forces obtained from the constant-velocity simulations show linear relationships with temperature. Work vs. extension profiles calculated at different temperatures show that the energy landscape corresponding to protein unfolding does not alter with temperature (within the temperature range considered here) until it reaches the intermediate state, but they shows different behavior after crossing the transition state, supporting a recent hypothesis based on an experimental study. The study also identifies hitherto unknown competing pathways for the unfolding of I27. Combining forced pulling along with thermal denaturation to examine protein folding is proposed as a powerful tool, especially in cases where the order parameter for unfolding is not simply the distance between the terminal residues [40]. We are currently investigating such changes in the unfolding pathways of proteins when the order parameter of end-to-end distance is not valid.

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